## PHYSICS OF MATERIALS



Physics School Autumn 2024

## **Series 11 Solution**

**13 December 2024** 

## **Exercise 1 Eutectic phase diagram**

The phase diagram is expressed in terms of weight. The law of levers gives us the following:

$$\begin{split} \frac{m_{\alpha}}{m_{\alpha}+m_{\beta}} &= \frac{X_{\beta}-X}{X_{\beta}-X_{\alpha}} \\ \frac{m_{\beta}}{m_{\alpha}+m_{\beta}} &= \frac{X-X_{\alpha}}{X_{\beta}-X_{\alpha}} \end{split}$$

At a temperature above the eutectic, we have the maximum solid phase in the liquid before solidification, which is given by:

$$\frac{m_{\beta}}{m_{L}+m_{\beta}} = \frac{80-60}{90-60} = 67\%$$
 of pro-eutectic  $\beta_{2}$  solid phase. Its concentration is 90% of the B element. The liquid has a eutectic concentration of 60%.

Right after the eutectic temperature T<sub>3</sub>, the liquid (that has the composition of the eutectic L2 with 60% of B) solidifies in two phases  $\alpha(30\%B) + \beta(90\%B)$ . Their weight ratio is given by:

$$\frac{m_{\alpha}}{m_{\alpha} + m_{\beta}} = \frac{90 - 60}{90 - 30} = 50\%$$

$$\frac{m_{\beta}}{m_{\alpha} + m_{\beta}} = \frac{60 - 30}{90 - 30} = 50\%$$

In the end, we have the following:

$$67\% + 0.5 \cdot 33\% = 83\%$$
 of  $\beta_{\text{phase}}$  and 17% of  $\alpha_{\text{phase}}$ .

The calculations at equilibrium for the temperature  $T_3$  give a decomposition in phases  $\alpha(30\%B) + \beta(90\%B)$  of which the weight ratios are:

$$\frac{m_{\alpha}}{m_{\alpha} + m_{\beta}} = \frac{90 - 80}{90 - 30} = 17\%$$

$$\frac{m_{\beta}}{m_{\alpha} + m_{\beta}} = \frac{80 - 30}{90 - 30} = 83\%$$

## Exercise 2 Iron-Carbon phase diagram

The eutectoid decomposition gives two phases: the  $\alpha$ -ferrite and the cementite Fe<sub>3</sub>C. The composition of the eutectoid is given by:

$$m_{\alpha} = \frac{X_{Fe_{3}C} - X}{X_{Fe_{3}C} - X_{\alpha}} (1 \, kg) = \frac{6.69 - 0.77}{6.69 - 0.02} = 885 \, g$$

$$m_{Fe_3C} = \frac{X - X_{\alpha}}{X_{Fe_3C} - X_{\alpha}} (1 \, kg) = \frac{0.77 - 0.02}{6.69 - 0.02} = 115 \, g$$

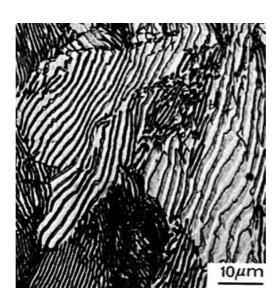


Figure 11-1: The structure of the steel's eutectoid is lamellar (like eutectic phases). We call this phase pearlite. This phase appears in an optical microscope as a dark color and pearl reflections (optical diffraction) from which its name derives.

When hypo-eutectoid steel (C<0.5wt%) is cooled, pro-eutectoid ferrite phase forms (see Fig. 11-2), and we can calculate its quantity with the phase diagram at equilibrium for 728°C.

$$m_{\alpha} = \frac{X_{\gamma} - X}{X_{\gamma} - X_{\alpha}} (1 \, kg) = \frac{0.77 - 0.5}{0.77 - 0.02} = 360 \, g$$

The remaining austenite (640 g) decomposes at 727°C, creating pearlite with the weight fractions calculated previously for the eutectoid composition. The calculation at equilibrium gives the final partition between ferrite and cementite. All of the cementite concentration is contained within the pearlitic structure.

$$m_{\alpha} = \frac{X_{Fe_{3}C} - X}{X_{Fe_{3}C} - X_{\alpha}} (1 \, kg) = \frac{6.69 - 0.5}{6.69 - 0.02} = 930 \, g$$

$$m_{Fe_{3}C} = \frac{X - X_{\alpha}}{X_{Fe_{3}C} - X_{\alpha}} (1 \, kg) = \frac{0.5 - 0.02}{6.69 - 0.02} = 70 \, g$$

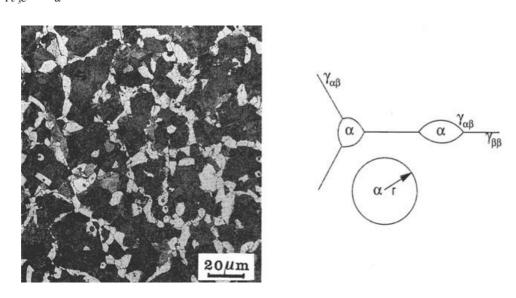


Fig. 11. 2 Formation mechanism of the pro-eutectoid ferrite (light colored) in the austenite. In the figure on the right, the dark phase is the pearlite arising from the austenite decomposition.

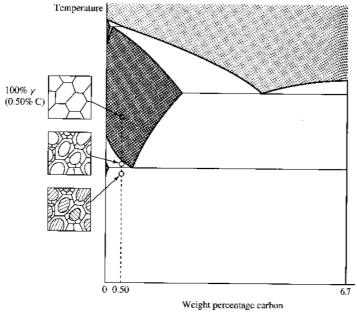


Fig. 11-3 Development of the microstructure of hypo-eutectoid steel.